Syllabus

Cambridge O Level Additional Mathematics Syllabus code 4037 For examination in June and November 2011



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1. Introduction

1.1 Why choose Cambridge?

University of Cambridge International Examinations (CIE) is the world's largest provider of international qualifications. Around 1.5 million students from 150 countries enter Cambridge examinations every year. What makes educators around the world choose Cambridge?

Developed for an international audience

International O Levels have been designed specially for an international audience and are sensitive to the needs of different countries. These qualifications are designed for students whose first language may not be English and this is acknowledged throughout the examination process. The curriculum also allows teaching to be placed in a localised context, making it relevant in varying regions.

Recognition

Cambridge O Levels are internationally recognised by schools, universities and employers as equivalent to UK GCSE. They are excellent preparation for A/AS Level, the Advanced International Certificate of Education (AICE), US Advanced Placement Programme and the International Baccalaureate (IB) Diploma. CIE is accredited by the UK Government regulator, the Qualifications and Curriculum Authority (QCA). Learn more at www.cie.org.uk/recognition.

Support

CIE provides a world-class support service for teachers and exams officers. We offer a wide range of teacher materials to Centres, plus teacher training (online and face-to-face) and student support materials. Exams officers can trust in reliable, efficient administration of exams entry and excellent, personal support from CIE Customer Services. Learn more at **www.cie.org.uk/teachers**.

Excellence in education

Cambridge qualifications develop successful students. They not only build understanding and knowledge required for progression, but also learning and thinking skills that help students become independent learners and equip them for life.

Not-for-profit, part of the University of Cambridge

CIE is part of Cambridge Assessment, a not-for-profit organisation and part of the University of Cambridge. The needs of teachers and learners are at the core of what we do. CIE invests constantly in improving its qualifications and services. We draw upon education research in developing our qualifications.

1. Introduction

1.2 Why choose Cambridge O Level Additional Mathematics?

International O Levels are established qualifications that keep pace with educational developments and trends. The International O Level curriculum places emphasis on broad and balanced study across a wide range of subject areas. The curriculum is structured so that students attain both practical skills and theoretical knowledge.

Cambridge O Level Additional Mathematics is recognised by universities and employers throughout the world as proof of mathematical knowledge and understanding. Successful Cambridge O Level Additional Mathematics candidates gain lifelong skills, including:

- the further development of mathematical concepts and principles
- the extension of mathematical skills and their use in more advanced techniques
- · an ability to solve problems, present solutions logically and interpret results
- a solid foundation for further study.

Students may also study for a Cambridge O Level in Mathematics and in Statistics. In addition to Cambridge O Levels, CIE also offers Cambridge IGCSE and International A & AS Levels for further study in Mathematics as well as other maths-related subjects. See **www.cie.org.uk** for a full list of the qualifications you can take.

1.3 How can I find out more?

If you are already a Cambridge Centre

You can make entries for this qualification through your usual channels, e.g. your regional representative, the British Council or CIE Direct. If you have any queries, please contact us at **international@cie.org.uk**.

If you are not a Cambridge Centre

You can find out how your organisation can become a Cambridge Centre. Email either your local British Council representative or CIE at **international@cie.org.uk**. Learn more about the benefits of becoming a Cambridge Centre at **www.cie.org.uk**.

2. Assessment at a glance

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All candidates will take two written papers.

The syllabus content will be assessed by Paper 1 and Paper 2.

Paper 1	Duration	Marks
10–12 questions of various lengths		
There will be no choice of question except that the last question will consist of two alternatives, only one of which must be answered. The mark allocations for the last question will be in the range of 10–12 marks.	2 hours	80

Paper 2	Duration	Marks
10–12 questions of various lengths		
There will be no choice of question except that the last question will consist of two alternatives, only one of which must be answered. The mark allocations for the last question will be in the range of 10–12 marks.	2 hours	80

Calculators

The syllabus assumes that candidates will be in possession of a silent electronic calculator with scientific functions for both papers. The General Regulations concerning the use of electronic calculators are contained in the *Handbook for Centres*.

Mathematical Instruments

Apart from the usual mathematical instruments, candidates may use flexicurves in this examination.

Mathematical Notation

Attention is drawn to the list of mathematical notation at the end of this booklet.

3. Syllabus aims and assessment

3.1 Aims

The aims of the syllabus listed below are not in order of priority. The aims are to enable candidates to:

- consolidate and extend their elementary mathematical skills, and use these in the context of more advanced techniques
- further develop their knowledge of mathematical concepts and principles, and use this knowledge for problem solving
- appreciate the interconnectedness of mathematical knowledge
- acquire a suitable foundation in mathematics for further study in the subject or in mathematics related subjects
- devise mathematical arguments and use and present them precisely and logically
- integrate information technology (IT) to enhance the mathematical experience
- develop the confidence to apply their mathematical skills and knowledge in appropriate situations
- develop creativity and perseverance in the approach to problem solving
- derive enjoyment and satisfaction from engaging in mathematical pursuits, and gain an appreciation of the beauty, power and usefulness of mathematics.

3.2 Assessment objectives

The examination will test the ability of candidates to:

- recall and use manipulative technique
- interpret and use mathematical data, symbols and terminology
- comprehend numerical, algebraic and spatial concepts and relationships
- recognise the appropriate mathematical procedure for a given situation
- formulate problems into mathematical terms and select and apply appropriate techniques of solution.

3.3 Exam combinations

A candidate can combine this syllabus in an exam session with any other CIE syllabus, except:

0606 IGCSE Additional Mathematics

Please note that O Level, Cambridge International Level1/Level 2 Certificate and IGCSE syllabuses are at the same level.

Knowledge of the content of CIE's Ordinary level Syllabus D (or an equivalent Syllabus) is assumed. O Level material which is not repeated in the syllabus below will not be tested directly but it may be required in response to questions on other topics.

Proofs of results will not be required unless specifically mentioned in the syllabus.

Candidates will be expected to be familiar with the scientific notation for the expression of compound units e.g. 5 ms⁻¹ for 5 metres per second.

Theme or topic	Curriculum objectives		
	Candidates should be able to:		
1. Set language and notation	 use set language and notation, and Venn diagrams to describe sets and represent relationships between sets as follows: A = {x: x is a natural number} 		
	$B = \{(x, y) \colon y = mx + c\}$		
	$C = \{x: a \le x \le b\}$		
	$D = \{a, b, c,\}$	$D = \{a, b, c,\}$	
	understand and use the following notation:		
	Union of A and B	$A \cup B$	
	Intersection of A and B	$A \cap B$	
	Number of elements in set A	n(A)	
	"is an element of"	€	
	"is not an element of"	∉	
	Complement of set A	A'	
	The empty set	Ø	
	Universal set	E	
	A is a subset of B	$A \subseteq B$	
	A is a proper subset of B	$A \subset B$	
	A is not a subset of B	A⊈B	
	A is not a proper subset of	$A \not\subset B$	

Theme or topic	Curriculum objectives		
2. Functions	understand the terms: function, domain, range (image set), one-one function, inverse function and composition of functions functions		
	• use the notation $f(x) = \sin x$, $f: x \mapsto \lg x$, $(x > 0)$, $f^{-1}(x)$ and $f^{2}(x) = f(f(x))$		
	• understand the relationship between $y = f(x)$ and $y = f(x) $, where $f(x)$ may be linear, quadratic or trigonometric		
	explain in words why a given function is a function or why it does not have an inverse		
	find the inverse of a one-one function and form composite functions		
	use sketch graphs to show the relationship between a function and its inverse		
3. Quadratic functions	• find the maximum or minimum value of the quadratic function $f: x \mapsto ax^2 + bx + c$ by any method		
	use the maximum or minimum value of f(x) to sketch the graph or determine the range for a given domain		
	• know the conditions for $f(x) = 0$ to have:		
	(i) two real roots, (ii) two equal roots, (iii) no real roots		
	and the related conditions for a given line to		
	(i) intersect a given curve, (ii) be a tangent to a given curve, (iii) not intersect a given curve		
	solve quadratic equations for real roots and find the solution set for quadratic inequalities		
4. Indices and surds	perform simple operations with indices and with surds, including rationalising the denominator		
5. Factors of polynomials	know and use the remainder and factor theorems		
	find factors of polynomials		
	solve cubic equations		
6. Simultaneous equations	solve simultaneous equations in two unknowns with at least one linear equation		

Theme or topic	Curriculum objectives
7. Logarithmic and exponential functions	 know simple properties and graphs of the logarithmic and exponential functions including ln x and e^x (series expansions are not required)
	know and use the laws of logarithms (including change of base of logarithms)
	• solve equations of the form $a^x = b$
8. Straight line graphs	• interpret the equation of a straight line graph in the form $y = mx + c$
	• transform given relationships, including $y = ax^n$ and $y = Ab^x$, to straight line form and hence determine unknown constants by calculating the gradient or intercept of the transformed graph
	solve questions involving mid-point and length of a line
	 know and use the condition for two lines to be parallel or perpendicular
9. Circular measure	solve problems involving the arc length and sector area of a circle, including knowledge and use of radian measure
10. Trigonometry	 know the six trigonometric functions of angles of any magnitude (sine, cosine, tangent, secant, cosecant, cotangent) understand amplitude and periodicity and the relationship between graphs of e.g. sin x and sin 2x draw and use the graphs of
	$y = a \sin(bx) + c$
	$y = a \cos(bx) + c$
	$y = a \tan (bx) + c$
	where a, b are positive integers and c is an integer
	use the relationships
	$\frac{\sin A}{\cos A} = \tan A, \frac{\cos A}{\sin A} = \cot A, \sin^2 A + \cos^2 A = 1,$
	$\sec^2 A = 1 + \tan^2 A$, $\csc^2 A = 1 + \cot^2 A$
	and solve simple trigonometric equations involving the six trigonometric functions and the above relationships (not including general solution of trigonometric equations) • prove simple trigonometric identities

Theme or topic	Curriculum objectives
11. Permutations and combinations	recognise and distinguish between a permutation case and a combination case
	 know and use the notation n! (with 0! = 1), and the expressions for permutations and combinations of n items taken r at a time
	answer simple problems on arrangement and selection (cases with repetition of objects, or with objects arranged in a circle or involving both permutations and combinations, are excluded)
12. Binomial expansions	 use the Binomial Theorem for expansion of (a + b)ⁿ for positive integral n use the general term (n) a^{n-r} b^r, 0 < r ≤ n
	(knowledge of the greatest term and properties of the coefficients is not required)
13. Vectors in 2 dimensions	• use vectors in any form, e.g. $\begin{pmatrix} a \\ b \end{pmatrix}$, \overrightarrow{AB} , \mathbf{p} , $a\mathbf{i} - b\mathbf{j}$
	know and use position vectors and unit vectors
	find the magnitude of a vector, add and subtract vectors and multiply vectors by scalars
	compose and resolve velocities
	use relative velocity, including solving problems on interception (but not closest approach)
14. Matrices	display information in the form of a matrix of any order and interpret the data in a given matrix
	solve problems involving the calculation of the sum and product (where appropriate) of two matrices and interpret the results
	calculate the product of a scalar quantity and a matrix
	use the algebra of 2 × 2 matrices (including the zero and identity matrix)
	calculate the determinant and inverse of a non-singular 2 × 2 matrix and solve simultaneous linear equations

Theme or topic	Curriculum objectives
15. Differentiation and integration	understand the idea of a derived function
	• use the notations $f'(x)$, $f''(x)$, $\frac{dy}{dx}$, $\frac{d^2y}{dx^2}$, $\left[= \frac{d}{dx} \left(\frac{dy}{dx} \right) \right]$
	use the derivatives of the standard functions
	x^n (for any rational n), $\sin x$, $\cos x$, $\tan x$, e^x , $\ln x$, together with constant multiples, sums and composite functions of these
	differentiate products and quotients of functions
	apply differentiation to gradients, tangents and normals, stationary points, connected rates of change, small increments and approximations and practical maxima and minima problems
	discriminate between maxima and minima by any method
	understand integration as the reverse process of differentiation
	• integrate sums of terms in powers of x , excluding $\frac{1}{x}$
	• integrate functions of the form $(ax + b)^n$ (excluding $n = -1$), e^{ax+b} , $\sin(ax + b)$, $\cos(ax + b)$
	evaluate definite integrals and apply integration to the evaluation of plane areas
	apply differentiation and integration to kinematics problems that involve displacement, velocity and acceleration of a particle moving in a straight line with variable or constant acceleration, and the use of x-t and v-t graphs

The list which follows summarises the notation used in the CIE's Mathematics examinations. Although primarily directed towards Advanced/HSC (Principal) level, the list also applies, where relevant, to examinations at O Level/S.C.

Mathematical Notation

1. Set Notation

$ \begin{array}{c} $	€	is an element of
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	∉	is not an element of
the number of elements in set A the empty set universal set the complement of the set A the complement of the set A the set of positive integers, $\{1, 2, 3,\}$ the set of integers $\{0, \pm 1, \pm 2, \pm 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of integers modulo n , $\{0, 1, 2,, n-1\}$ the set of rational numbers the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive real numbers $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$	$\{x_1, x_2, \ldots\}$	the set with elements x_1, x_2, \ldots
$\begin{array}{lll} \varnothing & \text{the empty set} \\ \& & \text{universal set} \\ A' & \text{the complement of the set } A \\ \mathbb{N} & \text{the set of positive integers, } \{1, 2, 3, \ldots\} \\ \mathbb{Z} & \text{the set of integers } \{0, \pm 1, \pm 2, \pm 3, \ldots\} \\ \mathbb{Z}^* & \text{the set of positive integers } \{1, 2, 3, \ldots\} \\ \mathbb{Z}_n & \text{the set of integers modulo } n, \{0, 1, 2, \ldots, n-1\} \\ \mathbb{Q} & \text{the set of rational numbers} \\ \mathbb{Q}^* & \text{the set of positive rational numbers, } \{x \in \mathbb{Q}: x > 0\} \\ \mathbb{R} & \text{the set of positive rational numbers and zero, } \{x \in \mathbb{Q}: x \geq 0\} \\ \mathbb{R}^* & \text{the set of positive real numbers } \{x \in \mathbb{R}: x > 0\} \\ \mathbb{R}^n & \text{the set of positive real numbers and zero } \{x \in \mathbb{R}: x \geq 0\} \\ \mathbb{R}^n & \text{the set of complex numbers} \\ \mathbb{C} & \text{the set of complex numbers} \\ \mathbb{C} & \text{the set of complex numbers} \\ \mathbb{C} & \text{is a proper subset of} \\ \mathbb{C} & \text{is not a subset of} \\ \mathbb{C} & \text{is not a subset of} \\ \mathbb{C} & \text{is not a proper subset of} $	{ <i>x</i> :}	the set of all x such that
universal set the complement of the set A the set of positive integers, $\{1, 2, 3,\}$ the set of integers $\{0, \pm 1, \pm 2, \pm 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of integers modulo n , $\{0, 1, 2,, n-1\}$ the set of rational numbers the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x > 0\}$ the real n tuples the set of complex numbers the set of complex numbers is a subset of is not a subset of is not a subset of union	n(A)	the number of elements in set A
the complement of the set A the set of positive integers, $\{1, 2, 3,\}$ the set of integers $\{0, \pm 1, \pm 2, \pm 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of integers modulo n , $\{0, 1, 2,, n-1\}$ the set of integers modulo n , $\{0, 1, 2,, n-1\}$ the set of rational numbers the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x \geq 0\}$ the set of positive real numbers and zero, $\{x \in \mathbb{R}: x \geq 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ the set of complex numbers c the set of complex numbers is a subset of is a proper subset of is not a subset of union	Ø	the empty set
the set of positive integers, $\{1, 2, 3,\}$ the set of integers $\{0, \pm 1, \pm 2, \pm 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of positive integers $\{1, 2, 3,\}$ the set of integers modulo n , $\{0, 1, 2,, n-1\}$ the set of rational numbers the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x \ge 0\}$ the set of positive real numbers the set of positive real numbers $\{x \in \mathbb{R}: x \ge 0\}$ the set of positive real numbers and zero $\{x \in \mathbb{R}: x \ge 0\}$ the real n tuples the set of complex numbers is a subset of is a proper subset of is not a subset of union	E	universal set
	$A^{'}$	the complement of the set A
	N	the set of positive integers, {1, 2, 3,}
\mathbb{Z}_n the set of integers modulo n , $\{0, 1, 2,, n-1\}$ \mathbb{Q} the set of rational numbers \mathbb{Q}^+ the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ \mathbb{Q}^0 the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x \geq 0\}$ \mathbb{R} the set of positive real numbers \mathbb{R}^+ the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ \mathbb{R}^n the real n tuples \mathbb{C} the set of complex numbers \subseteq is a subset of \subseteq is not a subset of $\not\subseteq$ is not a proper subset of \cup union	\mathbb{Z}	the set of integers $\{0, \pm 1, \pm 2, \pm 3, \ldots\}$
the set of rational numbers \mathbb{Q}^+ the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x \geq 0\}$ \mathbb{R}^+ the set of positive real numbers \mathbb{R}^+ the set of positive real numbers $\{x \in \mathbb{R}: x > 0\}$ \mathbb{R}^0 the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ \mathbb{R}^n the real n tuples \mathbb{C} the set of complex numbers \mathbb{C} is a subset of \mathbb{C} is a proper subset of \mathbb{C} is not a subset of \mathbb{C} is not a proper subset of \mathbb{C} is not a proper subset of	\mathbb{Z}^{+}	the set of positive integers {1, 2, 3,}
the set of positive rational numbers, $\{x \in \mathbb{Q}: x > 0\}$ \mathbb{Q}_0^+ the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x \geq 0\}$ \mathbb{R} the set of real numbers \mathbb{R}^+ the set of positive real numbers $\{x \in \mathbb{R}: x > 0\}$ \mathbb{R}^0 the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ \mathbb{R}^n the real n tuples \mathbb{C} the set of complex numbers \subseteq is a subset of \subseteq is a proper subset of $\not\subseteq$ is not a subset of $\not\subseteq$ is not a proper subset of $ oursign*$ union	\mathbb{Z}_n	the set of integers modulo n , $\{0, 1, 2,, n-1\}$
$\begin{array}{lll} \mathbb{Q}_0^+ & \text{the set of positive rational numbers and zero, } \{x \in \mathbb{Q}: x \geqslant 0\} \\ \mathbb{R} & \text{the set of real numbers} \\ \mathbb{R}^+ & \text{the set of positive real numbers } \{x \in \mathbb{R}: x > 0\} \\ \mathbb{R}_0^+ & \text{the set of positive real numbers and zero } \{x \in \mathbb{R}: x \geqslant 0\} \\ \mathbb{R}^n & \text{the real } n \text{ tuples} \\ \mathbb{C} & \text{the set of complex numbers} \\ \subseteq & \text{is a subset of} \\ \subseteq & \text{is a proper subset of} \\ \not\subseteq & \text{is not a subset of} \\ \not\subseteq & \text{is not a proper subset of} \\ \\ \cup & \text{union} \\ \end{array}$	\mathbb{Q}	the set of rational numbers
\mathbb{R} the set of real numbers \mathbb{R}^+ the set of positive real numbers $\{x \in \mathbb{R}: x > 0\}$ \mathbb{R}^n the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ \mathbb{R}^n the real n tuples \mathbb{C} the set of complex numbers \subseteq is a subset of \subseteq is a proper subset of $\not\subseteq$ is not a subset of $\not\subseteq$ is not a proper subset of \cup union	$\mathbb{Q}^{^{+}}$	the set of positive rational numbers, $\{x \in \mathbb{Q}: x \geq 0\}$
$\mathbb{R}^+ \qquad \qquad \text{the set of positive real numbers } \{x \in \mathbb{R}: x > 0\}$ $\mathbb{R}^n \qquad \qquad \text{the real } n \text{ tuples}$ $\mathbb{C} \qquad \qquad \text{the set of complex numbers}$ $\subseteq \qquad \qquad \text{is a subset of}$ $\subseteq \qquad \qquad \text{is a proper subset of}$ $\not\subseteq \qquad \qquad \text{is not a subset of}$ $\not\subseteq \qquad \qquad \text{is not a proper subset of}$ $\vee \qquad \qquad \text{union}$	$\mathbb{Q}_0^{\scriptscriptstyle +}$	the set of positive rational numbers and zero, $\{x \in \mathbb{Q}: x \ge 0\}$
\mathbb{R}^+_0 the set of positive real numbers and zero $\{x \in \mathbb{R}: x \geq 0\}$ \mathbb{R}^n the real n tuples \mathbb{C} the set of complex numbers \subseteq is a subset of \subseteq is a proper subset of \nsubseteq is not a subset of \nsubseteq is not a proper subset of \bigvee union	\mathbb{R}	the set of real numbers
\mathbb{R}^n the real n tuples \mathbb{C} the set of complex numbers \subseteq is a subset of \subseteq is a proper subset of \nsubseteq is not a subset of \nsubseteq is not a proper subset of \bigvee union	$\mathbb{R}^{\scriptscriptstyle +}$	the set of positive real numbers $\{x \in \mathbb{R}: x > 0\}$
the set of complex numbers is a subset of is a proper subset of is not a subset of is not a proper subset of union the set of complex numbers is a subset of union	$\mathbb{R}_0^{\scriptscriptstyle +}$	the set of positive real numbers and zero $\{x \in \mathbb{R}: x \ge 0\}$
is a subset of is a proper subset of is not a subset of is not a proper subset of union is not a proper subset of	\mathbb{R}^n	the real n tuples
is a proper subset of is not a subset of is not a proper subset of union is not a proper subset of	\mathbb{C}	the set of complex numbers
	\subseteq	is a subset of
	C	is a proper subset of
Union	⊈	is not a subset of
	⊄	is not a proper subset of
	\cup	union
	\cap	intersection

[*a*, *b*]

(a, b]

(a, b)

yRx

 $y \sim x$

oc.

the closed interval $\{x \in \mathbb{R}: a \le x \le b\}$

the interval $\{x \in \mathbb{R}: a \le x < b\}$

the interval $\{x \in \mathbb{R}: a < x \le b\}$

the open interval $\{x \in \mathbb{R}: a \le x \le b\}$

y is related to x by the relation R

y is equivalent to x, in the context of some equivalence relation

2. Miscellaneous Symbols

is equal to

is not equal to

is identical to or is congruent to

is approximately equal to

is isomorphic to is proportional to

<; ≪ is less than, is much less than

≤, ≯ is less than or equal to, is not greater than

>; >> is greater than, is much greater than

 \geqslant , \Leftrightarrow is greater than or equal to, is not less than

infinity

3. Operations

a+b a plus b

a-b a minus b

 $a \times b$, ab, a.b a multiplied by b

 $a \div b$, $\frac{a}{b}$, a/b a divided by b

a:b the ratio of a to b

 $\sum_{i=1}^{n} a_i \qquad \qquad a_1 + a_2 + \ldots + a_n$

the positive square root of the real number a

the modulus of the real number a

n factorial for $n \in \mathbb{N}$ (0! = 1)

the binomial coefficient $\frac{n!}{r!(n-r)!}$, for $n, r \in \mathbb{N}$, $0 \le r \le n$

 $\frac{n(n-1)...(n-r+1)}{r!}, \text{ for } n \in \mathbb{Q}, r \in \mathbb{N}$

|a|

4. Functions

 \dot{X} , \ddot{X} , ...

function f
the value of the function f at x
${\bf f}$ is a function under which each element of set ${\bf A}$ has an image in set ${\bf B}$
the function f maps the element x to the element y
the inverse of the function f
the composite function of f and g which is defined by
$(g \circ f)(x)$ or $gf(x) = g(f(x))$
the limit of $f(x)$ as x tends to a
an increment of x
the derivative of y with respect to x
the n th derivative of y with respect to x
the first, second,, n th derivatives of $f(x)$ with respect to x
indefinite integral of y with respect to x
the definite integral of y with respect to x for values of x between a and b
the partial derivative of y with respect to x

5. Exponential and Logarithmic Functions

e	base of natural logarithms
e^x , $exp x$	exponential function of x
$\log_a x$	logarithm to the base a of x
$\ln x$	natural logarithm of x
lg x	logarithm of x to base 10

the first, second, \dots derivatives of x with respect to time

6. Circular and Hyperbolic Functions and Relations

sin, cos, tan,	ļ	the circular functions
cosec, sec, cot	J	the circular functions
sin ⁻¹ , cos ⁻¹ , tan ⁻¹ , cosec ⁻¹ , sec ⁻¹ , cot ⁻¹	}	the inverse circular relations
sinh, cosh, tanh, cosech, sech, coth	}	the hyperbolic functions
sinh ⁻¹ , cosh ⁻¹ , tanh ⁻¹ , cosech ⁻¹ , sech ⁻¹ , coth ⁻¹	}	the inverse hyperbolic relations

7. Complex Numbers

i	square root of -1
z	a complex number, $z = x + iy$
	$= r(\cos\theta + i\sin\theta), r \in \mathbb{R}_0^+$
	$=r\mathrm{e}^{\mathrm{i} heta},r\in\mathbb{R}_{0}^{+}$
Re z	the real part of z , Re $(x + iy) = x$
Im z	the imaginary part of z, $\operatorname{Im}(x + iy) = y$
	the modulus of z , $ x + iy = \sqrt{(x^2 + y^2)}$, $ r(\cos \theta + i \sin \theta) = r$
arg z	the argument of z , $arg(r(\cos\theta + i\sin\theta)) = \theta$, $-\pi < \theta \le \pi$
z*	the complex conjugate of z , $(x + iy)^* = x - iy$

8. Matrices

M	a matrix M
M^{-1}	the inverse of the square matrix ${f M}$
\mathbf{M}^{T}	the transpose of the matrix ${f M}$
det M	the determinant of the square matrix ${f M}$

9. Vectors

a	the vector a
\overrightarrow{AB}	the vector represented in magnitude and direction by the directed line segment $\it AB$
â	a unit vector in the direction of the vector ${f a}$
i, j, k	unit vectors in the directions of the cartesian coordinate axes
$ \mathbf{a} $	the magnitude of a
$ \overrightarrow{AB} $	the magnitude of \overrightarrow{AB}
a.b	the scalar product of ${\bf a}$ and ${\bf b}$
$\mathbf{a} \times \mathbf{b}$	the vector product of a and b

40 B 1 120 100 120	
10. Probability and Statistics	ovente.
A, B, C etc. $A \cup B$	events union of events A and B
	intersection of the events A and B
$A \cap B$	
P(A) A'	probability of the event A
	complement of the event A, the event 'not A'
P(A B)	probability of the event A given the event B
X, Y, R, etc.	random variables
<i>x, y, r,</i> etc.	values of the random variables <i>X, Y, R</i> , etc.
x_1, x_2, \ldots	observations
f_1, f_2, \dots	frequencies with which the observations x_1, x_2, \dots occur
p(x)	the value of the probability function $P(X = x)$ of the discrete
	random variable X
p_1, p_2, \ldots	probabilities of the values x_1, x_2, \dots of the discrete random
	variable X
$f(x), g(x), \ldots$	the value of the probability density function of the continuous
$\Gamma(\cdot)$ $C(\cdot)$	random variable X
$F(x), G(x), \dots$	the value of the (cumulative) distribution function $P(X \le x)$ of
E(IA)	the random variable X
E(X)	expectation of the random variable X
E[g(X)]	expectation of $g(X)$
Var(X)	variance of the random variable X
G(t)	the value of the probability generating function for a random
	variable which takes integer values
B(n, p)	binomial distribution, parameters n and p
$Po(\mu)$	Poisson distribution, mean μ
$N(\mu, \sigma^2)$	normal distribution, mean μ and variance σ^2
$\mu_{\frac{2}{2}}$	population mean
σ^2	population variance
σ	population standard deviation
\overline{x}	sample mean
s^2	unbiased estimate of population variance from a sample,
	$s^2 = \frac{1}{n-1} \sum_{x} \left(x - \overline{x} \right)^2$
ϕ	probability density function of the standardised normal variable
	with distribution N (0, 1)
Φ	corresponding cumulative distribution function
ρ	linear product-moment correlation coefficient for a population
r	linear product-moment correlation coefficient for a sample

covariance of X and Y

Cov(X, Y)

6. Resource list

The following titles represent some of the texts available in the UK at the time of printing this booklet. Teachers are encouraged to choose texts for class use which they feel will be of interest to their students and will support their own teaching style. ISBN numbers are provided wherever possible.

Author	Title	Date	Publisher	ISBN
Backhouse, J K & Houldsworth S PT	Essential Pure Mathematics: A First Course	1991	Longman	0582066581
Backhouse, J K & Houldsworth S PT	Pure Mathematics: A First Course	1985	Longman	0582353866
Bostock L & Chandler S	Mathematics: Core Maths for Advanced Level	2000	Nelson Thornes	0748755098
Bostock L & Chandler S	Mathematics: Pure Mathematics 1	1978	Nelson Thornes	0859500926
Emanuel, R	Pure Mathematics 1	2001	Longman	0582405505
Harwood Clarke, L	Additional Pure Mathematics	1980	Heinemann	0435511874
Talbert, J F	Additional Maths Pure and Applied	1995	Longman	0582265118

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